#### Multi-Agent Systems on Sensor Networks: A Distributed Reinforcement Learning Approach

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#### Presentation Structure

- Paper Objective
- Background
  - Multi-Agent Systems (MAS) & Wireless Sensor Networks (WSN)
  - Reinforcement Learning
- Distributed Reinforcement Learning (DRL) Approaches
- Simulations and Results
- Conclusion

## Paper Objective

- Goal
  - Use distributed reinforcement learning (DRL) in sensor networks
  - Decentralized cooperation among independent sensors
- Introduce three DRL approaches
  - IndLearners
  - Distributed Value Function (DVF) DRL
  - Optimistic DRL (OptDRL)
- Apply approaches in a simulation comparing:
  - Policy convergence
  - Energy consumption
  - Memory consumption

#### Multi-Agent Systems (MAS) in Wireless Sensor Networks (WSN)

- Multi-agent systems
  - Independent agents each acting upon the environment
  - Frequently changing environment dynamics
- Wireless sensor networks
  - Limited energy per sensor
  - Sensors can communicate with one another
    - Incurs energy costs
  - May or may not have a central hub
    - Centralized or decentralized
- Decentralization
  - Reduces energy consumption
  - Scalable
  - Natural implementation



#### Reinforcement Learning Overview





 $\mathcal{M} = (\mathcal{S}, \mathcal{A}, \mathcal{P}, \mathcal{R})$   $\left| \begin{array}{l} \mathcal{S} \text{ is a discrete set of states} \\ \mathcal{A} \text{ is a discrete set of actions} \\ \mathcal{P} : \mathcal{S} \times \mathcal{A} \to \mathcal{S} \\ P_{ss'}^a = Prob(s_{t+1} = s' | s_t = s, a_t = a) \\ \mathcal{R} : \mathcal{S} \times \mathcal{A} \to \mathbb{R} \\ R_{ss'}^a = E[r_{t+1} | s_{t+1} = s', s_t = s, a_t = a] \end{array} \right|$ 

#### Markov Decision Process (MDP)

- Markov Property
  - Future outcomes based only on current state
- MDP = RL problem that has Markov property
  - Defined as a 4-tuple

policy 
$$\pi : S \times \mathcal{A} \rightarrow [0..1]$$
  
 $R_t = \sum_{k=0}^{\infty} \gamma^k r_{t+k+1}$   
 $V^{\pi}(s, a) = E^{\pi} \{ R_t | s_t = s \}$   
 $= E^{\pi} \{ \sum_{k=0}^{\infty} \gamma^k r_{t+k+1} | s_t = s \}$ 

$$Q^{\pi}(s,a) = E^{\pi} \{ R_t | s_t = s, a_t = a \}$$
  
=  $E^{\pi} \{ \sum_{k=0}^{\infty} \gamma^k r_{t+k+1} | s_t = s, a_t = a \}$ 

$$Q^{\pi^*}(s,a) = \max_{\pi} Q^{\pi}(s,a) \; orall \; (s,a) \in \mathcal{S} imes \mathcal{A}$$

## Policies and Value Functions

- Policy
- Discounted rewards
- State-value function
- Action-value function
- Policy convergence

## Q-Learning

- Hold a 2D lookup table of [state, action] Q-values
- Update Q-values base on:

$$Q_{t+1}(s_t, a_t) = (1 - \alpha)Q_t(s_t, a_t) + \alpha \left( r_{t+1}(s_{t+1}) + \gamma \max_{a \in A} Q_t(s_{t+1}, a) \right)$$

# Fully Distributed Q-Learning (IndLearning)

- Rudimentary approach
- Used as baseline comparison
- No communication among agents
  - Each agent acts according to independent Q-learning
- $\,\circ\,$  Not guaranteed to converge on an optimal policy

$$\begin{aligned} Q_{t+1}^{i}(s_{t}^{i}, a_{t}^{i}) &= (1 - \alpha)Q_{t}^{i}(s_{t}^{i}, a_{t}^{i}) + \alpha \Big(r_{t+1}^{i}(s_{t+1}^{i}) \\ &+ \gamma \sum_{j \in Neigh(i)} f^{i}(j)V_{t}^{j}(s_{t+1}^{j}) \Big) \end{aligned}$$

$$V_{t+1}^{i}(s_{t}^{i}) = \max_{a \in A^{i}} Q_{t+1}^{i}(s_{t}^{i}, a)$$

$$f^{i}(j) = \begin{cases} \frac{1}{|Neigh(i)|}, & \text{if } Neigh(i) \neq 0; \\ 1, & \text{otherwise.} \end{cases}$$

#### Distributed Value Function (DVL) DRL

- Agents communicate information about value functions
- Communicates with all other nodes via the value function
  - Results in something like global reward but decentralized
- Algorithm

$$\mathcal{M} = (\mathcal{S}, \mathcal{A}, \mathcal{P}, \mathcal{R})$$
$$\mathcal{S} = \prod_{i=1}^{m} S^{i}$$
$$\mathcal{A} = \prod_{i=1}^{m} A^{i}$$
$$\mathcal{P} : \mathcal{S} \times \mathcal{S} \rightarrow [0, 1]$$
$$\mathcal{R} : \mathcal{S} \times \mathcal{A} \rightarrow \mathbb{R}$$

## Multi-Agent MDP (MAMDP)

- Extends the basic MDP from RL to multiple agents
  - Considers the state and action of every agent
- MAS state and action = vector of individual states and actions
- Similar 4-tuple to MDP

$$q_{t+1}^{i}(S_{t}, a_{t}^{i}) = \max\{q_{t}^{i}(S_{t}, a_{t}^{i}), (1 - \alpha)q_{t}^{i}(S_{t}, a_{t}^{i}) + \alpha \left(r_{t+1}^{i}(S_{t+1}) + \gamma \max_{a \in A^{i}} q_{t}^{i}(S_{t+1}, a)\right)\}$$

$$\Pi_{t+1}^{i}(S_{t}) = a_{t}^{i} \text{ iff } \max_{a \in A^{i}} q_{t}^{i}(S_{t}, a) \neq \max_{a \in A^{i}} q_{t+1}^{i}(S_{t}, a)$$

## Optimistic DRL (OptDRL)

 Uses two equations to ensure convergence of optimal policy

- $\circ~$  First equation
  - Q-function
  - Assumes other agents act optimally
- Second equation
  - Updates the policy only when there is an improvement
  - Introduces coordination among agents



## Simulations

5 stationary agents illuminating a 10x10 room

 $\circ$  Goals

- Fully illuminate a room
- Minimize energy consumption
- Agent actions
  - Lights off (No energy)
  - Lights low (Some energy)
  - Lights high (High energy)
- Agent states
  - Light level of the 5x5 grid around the agent
- Optimal policy
  - M1 turns off its light
  - All other agents turn on lights high

### Results

- Converged policies
  - IndLearners: all agents lights high (not optimal)
  - DVF and OptDRL: optimal
- Convergence time
  - DVF: 4400 iterations
  - OptDRL: 1200 iterations
- Energy consumption
  - OptDRL uses more energy for communication and computation than DVF
- Memory requirements

	Expression	Actual values
IndLearners	$ s^i   imes  A^i $	$2^{25} \times 3$
DVF	$ s^i   imes  A^i  +  s^i $	$2^{25} \times 4$
<b>OptDRL</b>	$ S  \times  A^i  +  S $	$2^{100} \times 4$