

The running time of PrimalityTest

(* The formulas for the running time derived in class *)

```
In[74]:= size = 31;
N[Floor[ $\sqrt{2^{\text{size}} - 1}$ ] - 1]
```

Out[75]= 46 339.

```
In[77]:= N[Ceiling[ $2^{\frac{\text{size}}{2}}$ ] - 2]
```

Out[77]= 46 339.

(* Below is a computation of the running time **in years** of PrimalityTest program posted on the class website on 1 terraFLOPS supercomputer, assumming the body of the loop consists of 1 floatin-point instruction *)

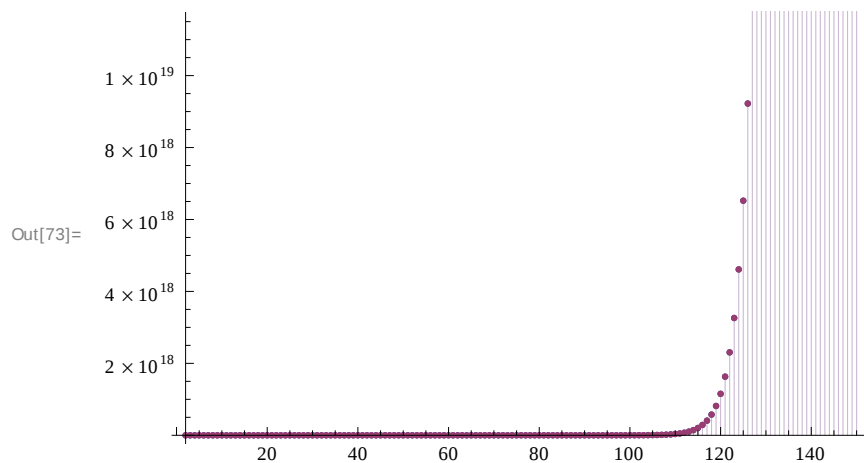
size = 150;

$n = N[\text{Ceiling}[2^{\frac{\text{size}}{2}}] - 2]$ (* formula we derived *);

$N[(n / (60(*\text{secs}*) \times 60(*\text{mins}*) \times 24(*\text{hrs}*) \times 365(*\text{days}*)) \times 10^{-15} \text{ (* 1 petaFLOPS*)}]$

Out[110]= 1.19796

```
In[73]:= DiscretePlot[{Floor[ $\sqrt{2^m - 1}$ ], Ceiling[ $2^{\frac{m}{2}}$ ] - 2}, {m, 2, 150}]
```



(* Below are auxiliary checks *)

$\text{Limit}\left[\frac{1}{2^{\frac{m}{2}}} \left(\text{Ceiling}\left[2^{\frac{m}{2}}\right] - 2\right), m \rightarrow \infty\right]$

1

$$\text{Limit}\left[\frac{1}{2^{\frac{m}{2}}}\left(\text{Floor}\left[\sqrt{2^m - 1}\right] - 1\right), m \rightarrow \infty\right]$$

1

$$\text{DiscretePlot}\left[\text{Floor}\left[\sqrt{2^m - 1}\right] - 1 - \left(\text{Ceiling}\left[2^{\frac{m}{2}}\right] - 2\right), \{m, 2, 439\}\right]$$

