

## RAID failures

n redundant disks

p - probability of fail for 1 disk  $0 < p < 1$

$p^n$  - probability of fail of the system (fail for all n disks)

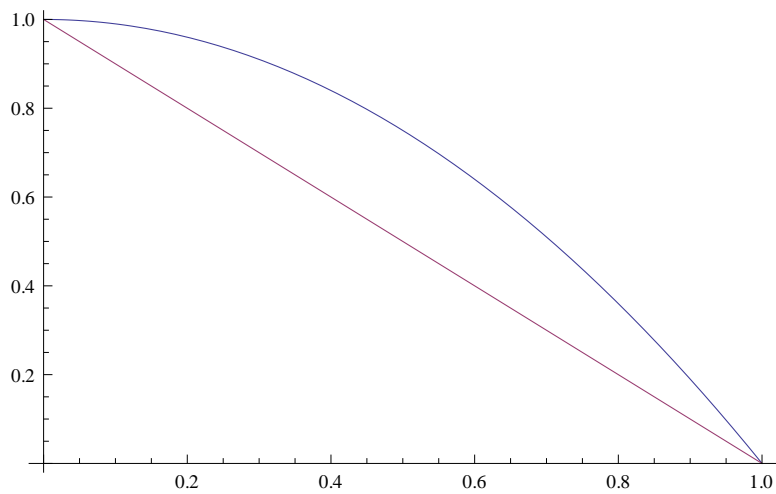
$1 - p^n$  - probability of **not** fail of the system

(**not** fail for some disk)

Probability of **not** fail of the system as a function of probability of fail of 1 disk

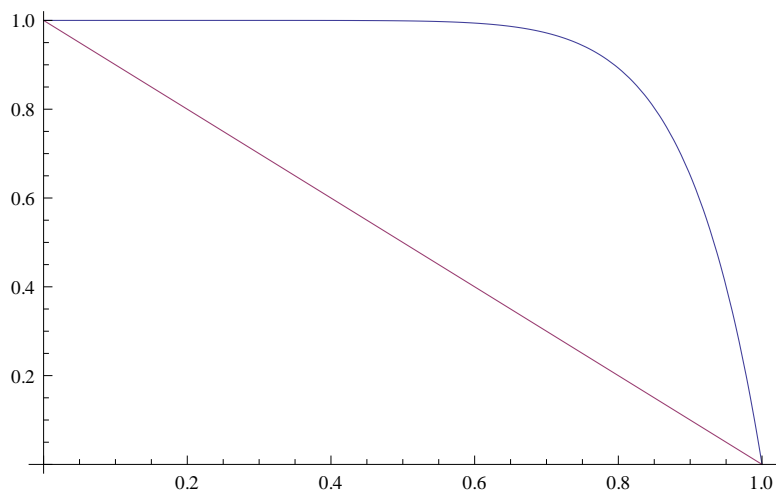
2 disks vs 1 disk

Plot  $[\{1 - p^2, 1 - p\}, \{p, 0, 1\}]$



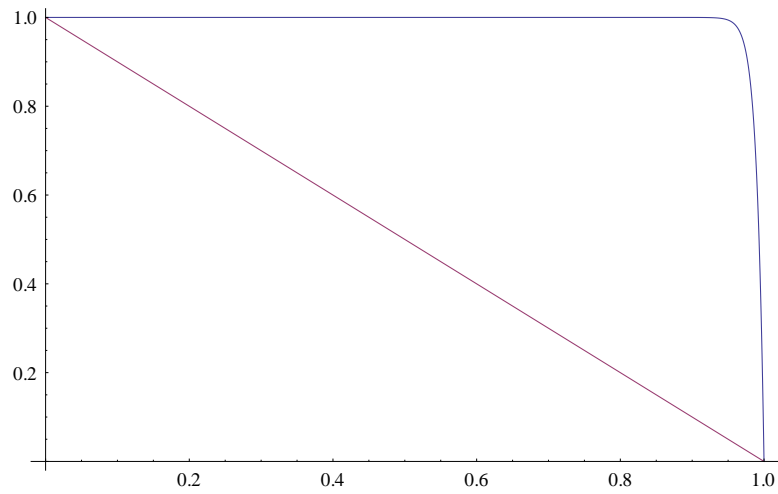
10 disks vs 1 disk

Plot  $[\{1 - p^{10}, 1 - p\}, \{p, 0, 1\}]$



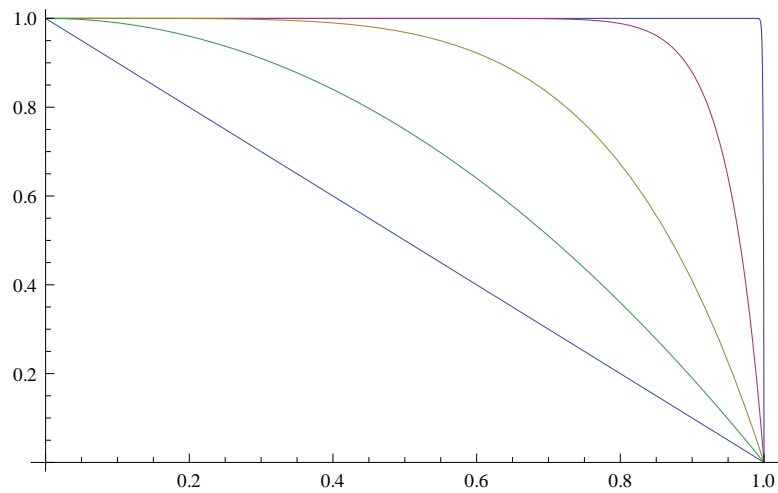
100 disks vs 1 disk

Plot  $\left[\{1 - p^{100}, 1 - p\}, \{p, 0, 1\}\right]$

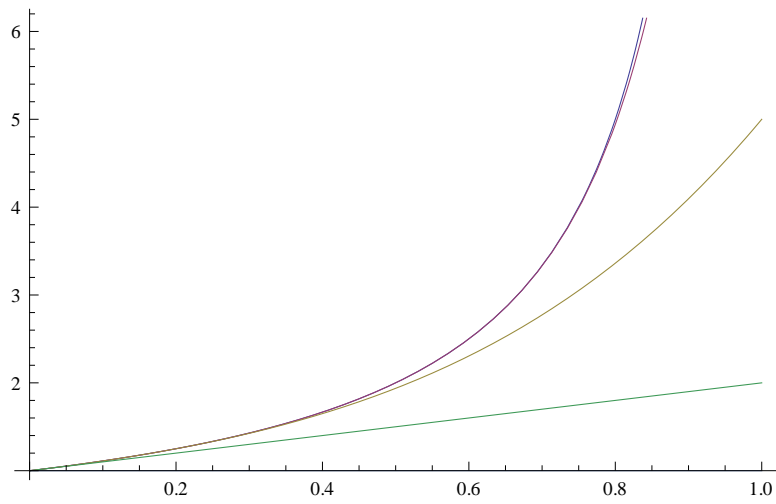


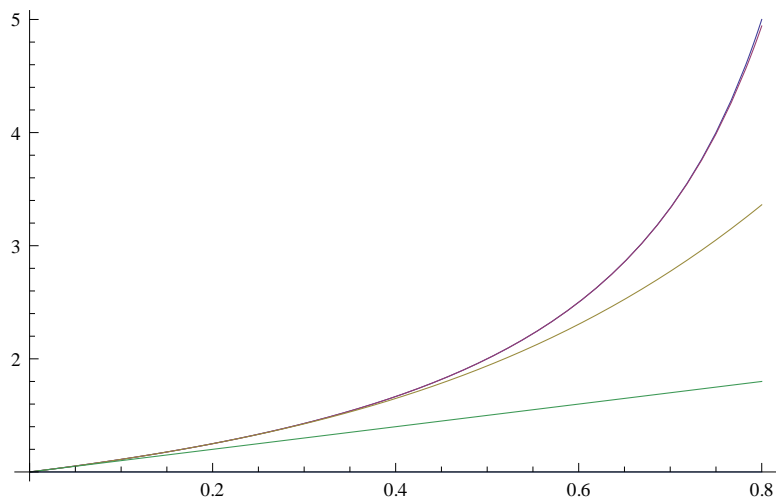
Comps for 1 disk, 2 disks, 5 disks, 20 disks, 1000 disks

Plot  $\left[\{1 - p^{1000}, 1 - p^{20}, 1 - p^5, 1 - p^2, 1 - p\}, \{p, 0, 1\}\right]$



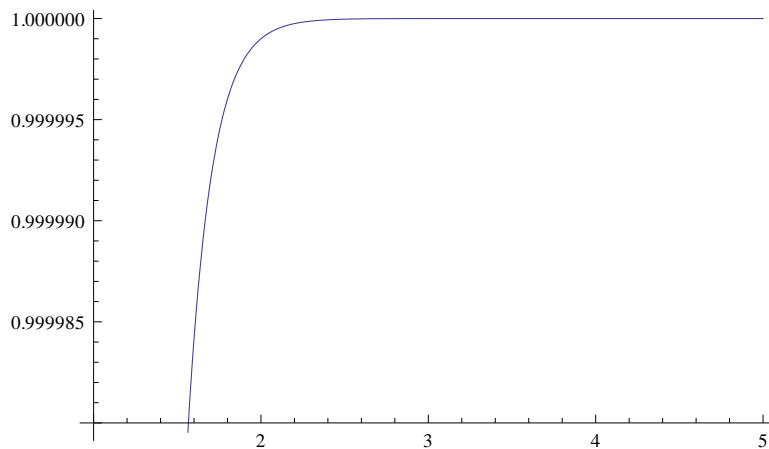
An increase of probability of **not** fail of a system relative to probability of **not** fail for a single disk as a function of probability of fail of a single disk.

$$\text{Plot}\left[\left\{\frac{1-p^{1000}}{1-p}, \frac{1-p^{20}}{1-p}, \frac{1-p^5}{1-p}, \frac{1-p^2}{1-p}, \frac{1-p}{1-p}\right\}, \{p, 0, 1\}\right]$$


$$\text{Plot}\left[\left\{\frac{1-p^{1000}}{1-p}, \frac{1-p^{20}}{1-p}, \frac{1-p^5}{1-p}, \frac{1-p^2}{1-p}, \frac{1-p}{1-p}\right\}, \{p, 0, .8\}\right]$$


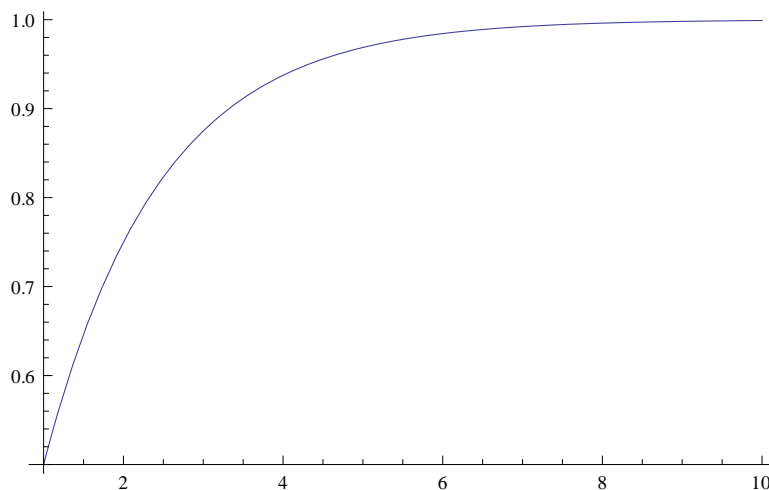
Probability of **not** fail of the system as a function of  $n$ ,  
given the probability of fail of 1 disk = .001

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Plot[{1 - .001^n}, {n, 1, 5}]
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Probability of **not** fail of the system as a function of  $n$ ,  
given the probability of fail of 1 disk = .5

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Plot[{1 - .5^n}, {n, 1, 10}]
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Now, in 3 D, the probability (ranging from 0 to 1) of **not** fail of the RAID as a  
function of the probability (ranging from 1 to 0) of fail of its single component  
(one disk) and the number (ranging from 1 to 18) of its components (disks) :

```
Plot3D[{1 - p^n}, {n, 1, 18}, {p, 0, 1}]
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